

# A New Standard of Ukraine: The Kupyna Hash Function

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## Abstract

The Kupyna hash function was approved as the new Ukrainian standard DSTU 7564:2014 in 2015. Main requirements for it were both high security level and good performance of software implementation on general-purpose 64-bit CPUs. The new hash function uses Davies-Meyer compression function based on Even-Mansour cipher construction. Kupyna is built on the transformations of the Kalyna block cipher (Ukrainian standard DSTU 7624:2014 [1, 2]). In this paper we present the adapted English translated specification of the Kupyna hash function as it is described in the national standard of Ukraine.

## 1 Introduction

Ukraine had been using the Commonwealth of Independent States (CIS) standard GOST 34.311-95 [3] (withdrawn Russian hash standard GOST R 34.11-94 [4]) as the main cryptographic hash function until 2015. Even now this transformation still provides acceptable level of practical security. However, its software implementation is significantly slower and less effective on modern platforms comparing to more recent solutions. In addition, theoretical attacks which are more effective than brute force were discovered [5]. Other CIS countries adopted newer standards instead of GOST R 34.11-94.

The new Ukrainian hash standard DSTU 7564:2014 [6] was developed based on a conservative approach using verified cryptographic constructions [7, 8, 9]. The

new hash function uses the Davies-Meyer compression function based on the Even-Mansour scheme. Internal permutations are built on the transformations of the Kalyna block cipher (the Ukrainian standard DSTU 7624:2014 [1, 2]).

The new standard defines both the hash function and its additional mode for message authentication code generation. In this paper we describe an adapted version of the specification of the Kupyna hash function as it is given in the national standard of Ukraine.

## 2 Symbols and notations

The following notations are used for the description.

$0x$	- a prefix of numbers given in the hexadecimal notation;
$GF(2^8)$	- the finite field with the irreducible polynomial $f(x) = x^8 + x^4 + x^3 + x^2 + 1$ ;
$\oplus$	- logical exclusive OR (XOR) operation for binary vectors;
$\otimes$	- vector multiplication over the finite field;
$\ll$	- the left shift of the fixed length sequence (to the most significant symbols); the least significant symbols are filled with 0's; number of symbols to be shifted is defined by the second argument;
$\gg$	- the cyclic shift (rotation) right of the fixed length sequence (the least significant symbols are moved to the most significant positions);
$(a_0, a_1, \dots, a_k)^T$	- transposition of the row vector $(a_0, a_1, \dots, a_k)$ into the column $\begin{pmatrix} a_0 \\ a_1 \\ \dots \\ a_k \end{pmatrix}$ ;
$a \bmod b$	- a non-negative remainder after dividing $a \in Z$ by $b \in Z^+$
$\omega_j^{(\nu)}, \varsigma_j^{(\nu)}$	- iteration constants for $\nu^{th}$ round of $T_l^\oplus$ and $T_l^+$ transformations;
$H$	- the hash function defined in this description;
$H(IV, M)$	- a hash code of a message $M$ ;
$IV$	- an initialization vector;
$n$	- the length of the hash code, $n = 8 \cdot s$ , $s \in \{1, 2, \dots, 64\}$ ;
$l$	- the size of the hash function internal state, $l \in \{512, 1024\}$ ;
$M$	- a message for hashing;
$m_i$	- $i^{th}$ block of the message $M$ after padding;
$N$	- the length (in bits) of the message $M$ without padding;
$R_{l,r}(X)$	- the function that returns $r$ most significant bits from the input sequence $X$ of $l$ -bit length;
$T_l^\oplus, T_l^+$	- the bijective mappings $T_l^\oplus, T_l^+ : V_l \rightarrow V_l$ , $l \in \{512, 1024\}$ (permutations) that transform an input block of $l$ bit length into output block of the same length;
$t$	- the number of rounds (iterations) in $T_l^\oplus$ and $T_l^+$ transformations;
$k$	- the number of blocks in the message $M$ , including padding;
$Z^+$	- the set of positive integers;

$V_j$	- $j$ -dimensional vector space over $GF(2)$ , $j \in Z^+$ ;
$+$	- addition operation defined in $Z_{2^{64}}$ ;
$V_j$	- $j$ -dimensional vector space over $GF(2)$ , $j \geq 1$ ;
$\Xi \circ \Lambda$	- a sequential application of transformations $\Xi$ and $\Lambda$ ( $\Lambda$ is applied first);
$\prod_{i=1}^t \Lambda^{(i)}$	- a sequential application of the transformations $\Lambda^{(1)}$ , $\Lambda^{(2)}$ , ..., $\Lambda^{(t)}$ (the transformation $\Lambda^{(1)}$ is applied first);
Kupyna- $n$	- the notation for the hash function with the hash code of $n$ -bit length.

### 3 General parameters

The hash function  $H$  is an  $IV$ -dependent mapping of a message  $M$  into the hash code  $H(IV, M)$  such that

$$\begin{aligned} H^{(IV)} : V_N &\rightarrow V_n, \quad n \in \{8 \cdot s | s = 1, 2, \dots, 64\}, \\ M \in V_N, \quad N &\in \{0, 1, \dots, 2^{96} - 1\}, \\ IV \in V_l, \quad l &\in \{512, 1024\}. \end{aligned}$$

Hash function mode of operation for  $n \in \{8 \cdot s | s = 1, 2, \dots, 64\}$  is denoted as Kupyna- $n$ . The main recommended modes are Kupyna-256, Kupyna-384 and Kupyna-512.

### 4 Structure of the transformation $H$

Input message for hashing is always padded (see Section 5) to obtain the length, which is a multiple of the block size. After padding it is divided into the blocks  $m_1, m_2, \dots, m_k$  of  $l$ -bit length, which is defined as

$$l = \begin{cases} 512, & \text{if } 8 \leq n \leq 256, \\ 1024, & \text{if } 256 < n \leq 512. \end{cases}$$

A hash code is obtained accordingly to the following iterative procedure:

$$\begin{aligned} h_0 &= IV, \\ h_\nu &= T_l^\oplus(h_{\nu-1} \oplus m_\nu) \oplus T_l^+(m_\nu) \oplus h_{\nu-1}, \quad \nu = 1, 2, \dots, k, \\ H(IV, M) &= R_{l,n}(T_l^\oplus(h_k) \oplus h_k), \end{aligned}$$

where

$$IV = \begin{cases} 1 \ll 510, & \text{if } l = 512, \\ 1 \ll 1023, & \text{if } l = 1024, \end{cases} \quad IV \in V_l,$$

$T_l^\oplus$ ,  $T_l^+$  are bijective mappings of  $l$ -bit blocks (see Section 6),

$R_{l,n}(X)$  is a function that returns  $n$  most significant bits from the input block  $X$  of  $l$ -bit length ( $n < l$ ).

A structural scheme of the Kupyna hash function is depicted in Figure 1.

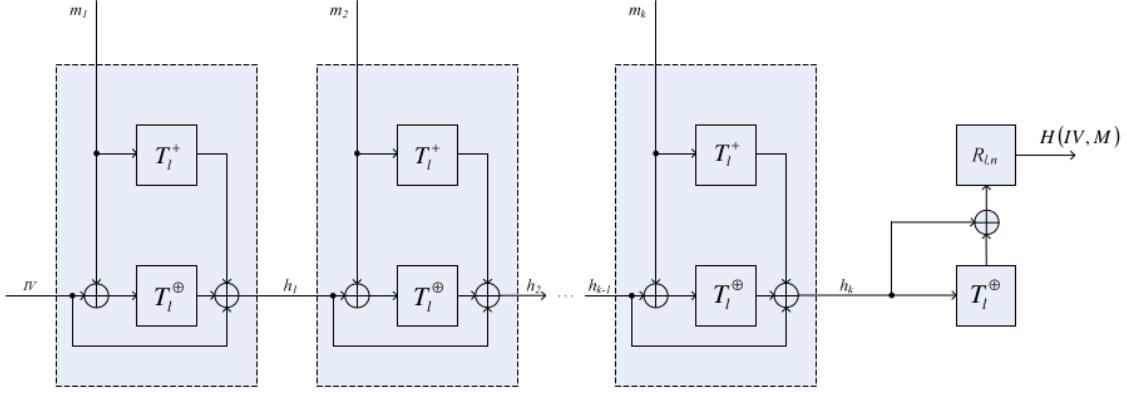


Figure 1: Structural scheme of the Kupyna hash function

Table 1: General parameters for Kupyna

Hash code length ( $n$ )	Internal state size ( $l$ )	Number of rounds ( $t$ )	Rows of the state matrix ( $c$ )
$8 \leq n \leq 256$	512	10	8
$256 < n \leq 512$	1024	14	16

## 5 Message padding

The hash function takes a message (a bit string) of  $N$  bits length as an input. Each message is padded regardless of its length. Padding follows the message and contains the single '1' bit, then  $d$  zero bits, where  $d = (-N - 97) \bmod l$ , and 96 bits containing the message length  $N$  (the least significant bits in the message length representation have smaller indexes, i.e. in the little-endian). As a result, the padded bit sequence has the length that is a multiple of the internal state  $l$ ,  $l \in \{512, 1024\}$ .

The maximum length of the message is limited to  $2^{96} - 1$  bits.

## 6 $T_l^\oplus$ and $T_l^+$ transformations

### General structure

Transformations  $T_l^\oplus$  and  $T_l^+$  are bijective mappings  $T_l^\oplus, T_l^+ : V_l \rightarrow V_l$ ,  $l \in \{512, 1024\}$ . Each mapping is implemented as iterative application of several functions that take input argument  $x \in V_l$  as a matrix of  $8 \times c$  bytes represented as elements of the  $GF(2^8)$  finite field.

The relation between the internal state size ( $l$ ), number of iterations ( $t$ ), number of the state matrix columns ( $c$ ) and the hash code length ( $n$ ) is given in Table 1.

The internal state matrix is denoted as  $G = (g_{i,j})$ ,  $g_{i,j} \in GF(2^8)$  where  $i = 0, 1, \dots, 7$ ,  $j = 0, 1, \dots, c - 1$ . It is filled in with input bytes  $B_1, B_2, \dots, B_{l/8}$  in a column-by-column order. Example for  $l = 512$  and  $c = 8$  is given in Figure 2. Output bytes are read from the state matrix in the same order.

$T_l^\oplus$  and  $T_l^+$  are defined as

Input byte sequence							
$B_1$	$B_9$	$B_{17}$	$B_{25}$	$B_{33}$	$B_{41}$	$B_{49}$	$B_{57}$
$B_2$	$B_{10}$	$B_{18}$	$B_{26}$	$B_{34}$	$B_{42}$	$B_{50}$	$B_{58}$
$B_3$	$B_{11}$	$B_{19}$	$B_{27}$	$B_{35}$	$B_{43}$	$B_{51}$	$B_{59}$
$B_4$	$B_{12}$	$B_{20}$	$B_{28}$	$B_{36}$	$B_{44}$	$B_{52}$	$B_{60}$
$B_5$	$B_{13}$	$B_{21}$	$B_{29}$	$B_{37}$	$B_{45}$	$B_{53}$	$B_{61}$
$B_6$	$B_{14}$	$B_{22}$	$B_{30}$	$B_{38}$	$B_{46}$	$B_{54}$	$B_{62}$
$B_7$	$B_{15}$	$B_{23}$	$B_{31}$	$B_{39}$	$B_{47}$	$B_{55}$	$B_{63}$
$B_8$	$B_{16}$	$B_{24}$	$B_{32}$	$B_{40}$	$B_{48}$	$B_{56}$	$B_{64}$

Internal state of the hash function							
$g_{0,0}$	$g_{0,1}$	$g_{0,2}$	$g_{0,3}$	$g_{0,4}$	$g_{0,5}$	$g_{0,6}$	$g_{0,7}$
$g_{1,0}$	$g_{1,1}$	$g_{1,2}$	$g_{1,3}$	$g_{1,4}$	$g_{1,5}$	$g_{1,6}$	$g_{1,7}$
$g_{2,0}$	$g_{2,1}$	$g_{2,2}$	$g_{2,3}$	$g_{2,4}$	$g_{2,5}$	$g_{2,6}$	$g_{2,7}$
$g_{3,0}$	$g_{3,1}$	$g_{3,2}$	$g_{3,3}$	$g_{3,4}$	$g_{3,5}$	$g_{3,6}$	$g_{3,7}$
$g_{4,0}$	$g_{4,1}$	$g_{4,2}$	$g_{4,3}$	$g_{4,4}$	$g_{4,5}$	$g_{4,6}$	$g_{4,7}$
$g_{5,0}$	$g_{5,1}$	$g_{5,2}$	$g_{5,3}$	$g_{5,4}$	$g_{5,5}$	$g_{5,6}$	$g_{5,7}$
$g_{6,0}$	$g_{6,1}$	$g_{6,2}$	$g_{6,3}$	$g_{6,4}$	$g_{6,5}$	$g_{6,6}$	$g_{6,7}$
$g_{7,0}$	$g_{7,1}$	$g_{7,2}$	$g_{7,3}$	$g_{7,4}$	$g_{7,5}$	$g_{7,6}$	$g_{7,7}$

Figure 2: Filling the internal state matrix for  $T_l^\oplus$  and  $T_l^+$

$$T_l^\oplus = \prod_{\nu=0}^{t-1} (\psi \circ \tau^{(l)} \circ \pi' \circ \kappa_\nu^{(l)}),$$

$$T_l^+ = \prod_{\nu=0}^{t-1} (\psi \circ \tau^{(l)} \circ \pi' \circ \eta_\nu^{(l)}),$$

where

$\kappa_\nu^{(l)}$  – the function of addition of the internal state with the iteration constant modulo 2,

$\eta_\nu^{(l)}$  – the function of addition of the internal state with the iteration constant modulo  $2^{64}$ ,

$\pi'$  – the layer of non-linear bijective mapping (S-box layer) that implements byte substitution,

$\tau_l$  – permutation of elements  $g_{i,j} \in GF(2^8)$  in the internal state (right rotation of the rows),

$\psi$  – the linear transformation (multiplication of the vector and matrix over the finite field).

Input argument  $x \in V_l$  and output value  $\chi(x) \in V_l$ ,  $\chi \in \{\kappa_\nu^{(l)}, \eta_\nu^{(l)}, \pi', \tau_l, \psi\}$ , are represented as matrices of  $8 \times c$  size (see Table 1).

## Addition with iteration constants

The  $\kappa_\nu^{(l)}$  function adds (modulo 2) a vector  $\omega_j^{(\nu)} = ((j \ll 4) \oplus \nu, 0, 0, 0, 0, 0, 0, 0)^T$ , where  $\omega_j^{(\nu)} \in V_{64}$ ,  $\nu$  is an iteration (round) number, to each column of the internal state matrix  $G = (g_{i,j})$ .

The  $\eta_\nu^{(l)}$  function adds (modulo  $2^{64}$ ) a vector  $\varsigma_j^{(\nu)} = (0xF3, 0xF0, 0xF0, 0xF0, 0xF0, 0xF0, 0xF0, 0xF0((c - 1 - j) \ll 4))^T$ , where  $\varsigma_j^{(\nu)} \in V_{64}$  and  $\nu$  is an iteration (round) number, to each column of the internal state matrix  $G = (g_{i,j})$ , and  $0xF3$  is the least significant byte of the  $\varsigma_j^{(\nu)}$  vector,  $g_{0,j}$  is the least significant byte of the  $G_j$  vector.

## Layer of non-linear bijective mapping

The  $\pi'$  function substitutes each element  $g_{i,j}$  of the internal state matrix  $G = (g_{i,j})$  by  $\pi_{i \bmod 4}(g_{i,j})$ , where  $\pi_s : V_8 \mapsto V_8$ ,  $s \in \{0, 1, 2, 3\}$ , are substitutions (S-boxes) given in Appendix A. For example, let  $g_{i,j}$  be  $0x23$ , then  $\pi_0(0x23) = 0x4F$ .

## Permutation of elements in the internal state

The function  $\tau_l$  performs cyclic right shift (rotation) for the rows in the state matrix  $G = (g_{i,j})$ . Rows with numbers  $i = 0, 1, \dots, 6$  of the matrix are rotated by  $i$  elements, and the row with the number 7 is rotated by 7 elements for  $l = 512$  and by 11 elements for  $l = 1024$ .

## Linear transformation

To perform the function  $\psi$  each element  $g_{i,j} \in V_8$  of the internal state matrix  $G$  is represented as an element of the finite field  $GF(2^8)$  formed by the irreducible polynomial  $\Upsilon(x) = x^8 + x^4 + x^3 + x^2 + 1$ , or  $0x11D$  in hexadecimal notation.

Each element of the resulting state matrix  $U = (u_{i,j})$  is calculated over  $GF(2^8)$  according to the formula

$$u_{i,j} = (v \gg i) \otimes G_j,$$

where  $v = (0x01, 0x01, 0x05, 0x01, 0x08, 0x06, 0x07, 0x04)$  is the vector that forms the circulant matrix with the MDS property, and  $G_j$  is the  $j^{th}$  column of the state matrix  $G$ .

The vector  $v$  consists of the hexadecimal constants (bytes) which are elements of the finite field  $GF(2^8)$ . The right circular shift is made with respect to elements of the set  $v$ .

## 7 Conclusions

Kupyna is a new Ukrainian standard of cryptographic hash function (DSTU 7564:2014). It uses Davies-Meyer compression function based on Even-Mansour block cipher construction. A message padding and a truncation of the result hash code are obligatory operations in Kupyna. Internal permutations are built on the transformations of the Kalyna block cipher (Ukrainian standard DSTU 7624:2014). Kupyna supports hash code length from 8 bits to 512 bits in 8-bit steps (called Kupyna- $n$ ). The recommended modes are Kupyna-256, Kupyna-384 and Kupyna-512. The description of the hash function given in this paper is an adapted English version of the Kupyna specification from the original standard.

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## A S-boxes for the Kupyna hash function (hexadecimal notation)

**Substitution  $\pi_0$**

A8	43	5F	06	6B	75	6C	59	71	DF	87	95	17	F0	D8	09
6D	F3	1D	CB	C9	4D	2C	AF	79	E0	97	FD	6F	4B	45	39
3E	DD	A3	4F	B4	B6	9A	0E	1F	BF	15	E1	49	D2	93	C6
92	72	9E	61	D1	63	FA	EE	F4	19	D5	AD	58	A4	BB	A1
DC	F2	83	37	42	E4	7A	32	9C	CC	AB	4A	8F	6E	04	27
2E	E7	E2	5A	96	16	23	2B	C2	65	66	0F	BC	A9	47	41
34	48	FC	B7	6A	88	A5	53	86	F9	5B	DB	38	7B	C3	1E
22	33	24	28	36	C7	B2	3B	8E	77	BA	F5	14	9F	08	55
9B	4C	FE	60	5C	DA	18	46	CD	7D	21	B0	3F	1B	89	FF
EB	84	69	3A	9D	D7	D3	70	67	40	B5	DE	5D	30	91	B1
78	11	01	E5	00	68	98	A0	C5	02	A6	74	2D	0B	A2	76
B3	BE	CE	BD	AE	E9	8A	31	1C	EC	F1	99	94	AA	F6	26
2F	EF	E8	8C	35	03	D4	7F	FB	05	C1	5E	90	20	3D	82
F7	EA	0A	0D	7E	F8	50	1A	C4	07	57	B8	3C	62	E3	C8
AC	52	64	10	D0	D9	13	0C	12	29	51	B9	CF	D6	73	8D
81	54	C0	ED	4E	44	A7	2A	85	25	E6	CA	7C	8B	56	80

**Substitution  $\pi_1$**

CE	BB	EB	92	EA	CB	13	C1	E9	3A	D6	B2	D2	90	17	F8
42	15	56	B4	65	1C	88	43	C5	5C	36	BA	F5	57	67	8D
31	F6	64	58	9E	F4	22	AA	75	0F	02	B1	DF	6D	73	4D
7C	26	2E	F7	08	5D	44	3E	9F	14	C8	AE	54	10	D8	BC
1A	6B	69	F3	BD	33	AB	FA	D1	9B	68	4E	16	95	91	EE
4C	63	8E	5B	CC	3C	19	A1	81	49	7B	D9	6F	37	60	CA
E7	2B	48	FD	96	45	FC	41	12	0D	79	E5	89	8C	E3	20
30	DC	B7	6C	4A	B5	3F	97	D4	62	2D	06	A4	A5	83	5F
2A	DA	C9	00	7E	A2	55	BF	11	D5	9C	CF	0E	0A	3D	51
7D	93	1B	FE	C4	47	09	86	0B	8F	9D	6A	07	B9	B0	98
18	32	71	4B	EF	3B	70	A0	E4	40	FF	C3	A9	E6	78	F9
8B	46	80	1E	38	E1	B8	A8	E0	0C	23	76	1D	25	24	05
F1	6E	94	28	9A	84	E8	A3	4F	77	D3	85	E2	52	F2	82
50	7A	2F	74	53	B3	61	AF	39	35	DE	CD	1F	99	AC	AD
72	2C	DD	D0	87	BE	5E	A6	EC	04	C6	03	34	FB	DB	59
B6	C2	01	F0	5A	ED	A7	66	21	7F	8A	27	C7	C0	29	D7

**Substitution  $\pi_2$** 

93	D9	9A	B5	98	22	45	FC	BA	6A	DF	02	9F	DC	51	59
4A	17	2B	C2	94	F4	BB	A3	62	E4	71	D4	CD	70	16	E1
49	3C	C0	D8	5C	9B	AD	85	53	A1	7A	C8	2D	E0	D1	72
A6	2C	C4	E3	76	78	B7	B4	09	3B	0E	41	4C	DE	B2	90
25	A5	D7	03	11	00	C3	2E	92	EF	4E	12	9D	7D	CB	35
10	D5	4F	9E	4D	A9	55	C6	D0	7B	18	97	D3	36	E6	48
56	81	8F	77	CC	9C	B9	E2	AC	B8	2F	15	A4	7C	DA	38
1E	0B	05	D6	14	6E	6C	7E	66	FD	B1	E5	60	AF	5E	33
87	C9	F0	5D	6D	3F	88	8D	C7	F7	1D	E9	EC	ED	80	29
27	CF	99	A8	50	0F	37	24	28	30	95	D2	3E	5B	40	83
B3	69	57	1F	07	1C	8A	BC	20	EB	CE	8E	AB	EE	31	A2
73	F9	CA	3A	1A	FB	0D	C1	FE	FA	F2	6F	BD	96	DD	43
52	B6	08	F3	AE	BE	19	89	32	26	B0	EA	4B	64	84	82
6B	F5	79	BF	01	5F	75	63	1B	23	3D	68	2A	65	E8	91
F6	FF	13	58	F1	47	0A	7F	C5	A7	E7	61	5A	06	46	44
42	04	A0	DB	39	86	54	AA	8C	34	21	8B	F8	0C	74	67

**Substitution  $\pi_3$** 

68	8D	CA	4D	73	4B	4E	2A	D4	52	26	B3	54	1E	19	1F
22	03	46	3D	2D	4A	53	83	13	8A	B7	D5	25	79	F5	BD
58	2F	0D	02	ED	51	9E	11	F2	3E	55	5E	D1	16	3C	66
70	5D	F3	45	40	CC	E8	94	56	08	CE	1A	3A	D2	E1	DF
B5	38	6E	0E	E5	F4	F9	86	E9	4F	D6	85	23	CF	32	99
31	14	AE	EE	C8	48	D3	30	A1	92	41	B1	18	C4	2C	71
72	44	15	FD	37	BE	5F	AA	9B	88	D8	AB	89	9C	FA	60
EA	BC	62	0C	24	A6	A8	EC	67	20	DB	7C	28	DD	AC	5B
34	7E	10	F1	7B	8F	63	A0	05	9A	43	77	21	BF	27	09
C3	9F	B6	D7	29	C2	EB	CO	A4	8B	8C	1D	FB	FF	C1	B2
97	2E	F8	65	F6	75	07	04	49	33	E4	D9	B9	D0	42	C7
6C	90	00	8E	6F	50	01	C5	DA	47	3F	CD	69	A2	E2	7A
A7	C6	93	0F	0A	06	E6	2B	96	A3	1C	AF	6A	12	84	39
E7	B0	82	F7	FE	9D	87	5C	81	35	DE	B4	A5	FC	80	EF
CB	BB	6B	76	BA	5A	7D	78	0B	95	E3	AD	74	98	3B	36
64	6D	DC	F0	59	A9	4C	17	7F	91	B8	C9	57	1B	E0	61